

Heinl 2015

Math 4 Honors

Unit 3 Test Review

Station #1: SAT Subject Test Math Questions

1. The function  $h$  is defined by  $h(x) = \frac{x^2 + 16}{x^2 - 9}$ . Which of the following values is NOT included in the domain of  $h$ ?

- a. -4
- b. -3
- c. 0
- d. 4
- e. 9

$$\begin{aligned} &= \frac{x^2 + 16}{(x+3)(x-3)} \\ &\quad \downarrow \qquad \downarrow \\ &x \neq -3 \quad x \neq 3 \end{aligned}$$

2. Which of the following expressions is equivalent to  $\frac{2y^5 + 6y^3}{y^4 + 3y^2}$ ?

- a.  $\frac{y}{3}$
- b.  $\frac{y+3}{2}$
- c.  $2y$
- d.  $2y + 3$
- e.  $\frac{2y^2}{y+3}$

$$\begin{aligned} &= \frac{2y^3(y^2+3)}{y^2(y^2+3)} \\ &= \frac{2y^3}{y^2} = 2y \end{aligned}$$

3. If  $\frac{x^2 - 4x + 3}{x - 1} = 5$ , then  $x =$

- a. 8
- b. 6
- c. 5
- d. 4
- e. 2

$$\begin{aligned} x^2 - 4x + 3 &= 5(x - 1) \\ x^2 - 4x + 3 &= 5x - 5 \\ -5x + 5 &\quad -5x + 5 \\ x^2 - 9x + 8 &= 0 \\ (x - 8)(x - 1) &= 0 \\ x = 8 \quad x = 1 &\text{ Extr.} \end{aligned}$$

4. What is  $\lim_{x \rightarrow -4} \frac{5x^2 + 22x + 8}{x^2 + 5x + 4}$ ?

- a. -3
- b. 0
- c. 3
- d. 6
- e. The limit does not exist.

$$\begin{aligned} &\frac{(5x + 2)(x + 4)}{(x + 1)(x + 4)} \\ &= \frac{5(-4) + 2}{-4 + 1} = \frac{-18}{-3} = 6 \end{aligned}$$

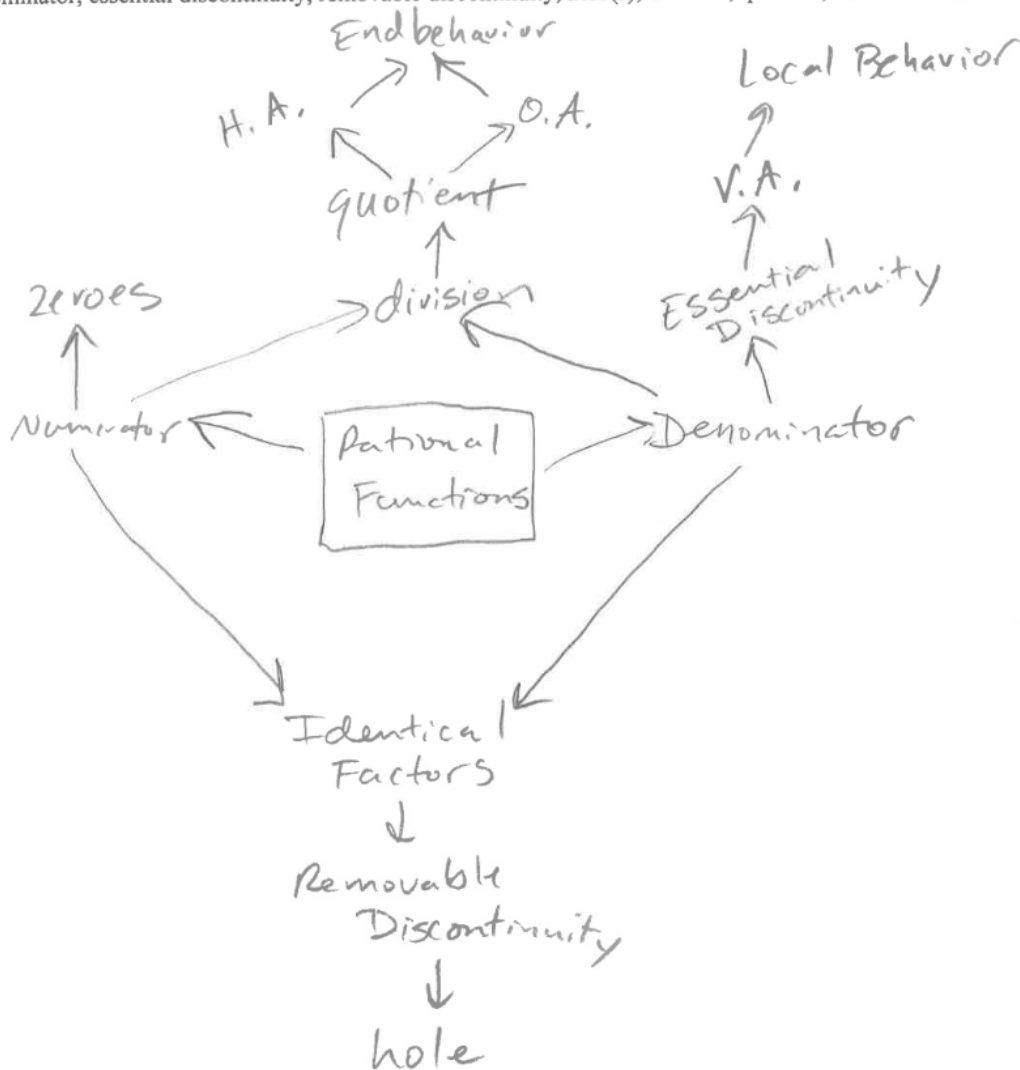
Math 4 Honors

Unit 3 Test Review

**Station #2: Rational Function Concept Map (or some other graphic organizer)**

Make a concept map (or some other graphic organizer) for *rational functions* and the vocabulary associated with them.

Vertical asymptote, horizontal asymptote, oblique asymptote, local behavior, end behavior, hole, numerator, denominator, essential discontinuity, removable discontinuity, zero(s), division, quotient, identical factors



Math 4 Honors

Unit 3 Test Review

**Station #3: Partial Fraction Decomposition**

1. Draw lines to match the rational expression with the form of its decomposition.

~~$\frac{x+21}{x(x^2-64)}$~~   $\rightarrow$   ~~$\frac{A}{x} + \frac{Bx+C}{x^2+64}$~~   
 $\frac{x+21}{x^2(x-64)}$   $\rightarrow$   $\frac{A}{x} + \frac{B}{x^2} + \frac{C}{x-64}$   
 $\frac{x+21}{x(x^2+64)}$   $\rightarrow$   $\frac{A}{x} + \frac{B}{x+8} + \frac{C}{x-8}$   
 $\frac{x+21}{x(x-64)^2}$   $\rightarrow$   $\frac{A}{x} + \frac{B}{x-64} + \frac{C}{(x-64)^2}$

2. Find the partial fraction decomposition of  $\frac{x+21}{x(x^2+64)}$ .

$$\cancel{x(x^2+64)} \left( \frac{x+21}{x(x^2+64)} \right) = \left( \frac{A}{x} + \frac{Bx+C}{x^2+64} \right) x(x^2+64)$$

$$x+21 = A(x^2+64) + (Bx+C)x$$

$$x+21 = Ax^2 + 64A + Bx^2 + Cx$$

$$x+21 = Ax^2 + Bx^2 + Cx + 64A$$

$$x+21 = (A+B)x^2 + Cx + 64A$$

$$A+B=0 \rightarrow B=-A$$

$$C=1 \quad B = \frac{-21}{64}$$

$$64A=21$$

$$A = \frac{21}{64}$$

$$\frac{x+21}{x(x^2+64)} = \frac{21}{64x} + \frac{-21x+1}{64(x^2+64)}$$

$$= \frac{21}{64x} + \frac{-21x+64}{64(x^2+64)}$$

Math 4 Honors

Unit 3 Test Review

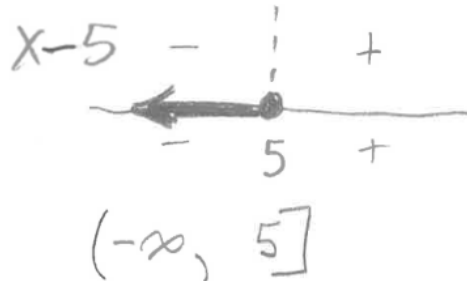
**Station #4: Solving Inequalities Using NLA**

Solve the following inequalities. Write your answers in interval notation.

1.  $\frac{x^2 - 25}{x + 5} \leq 0$

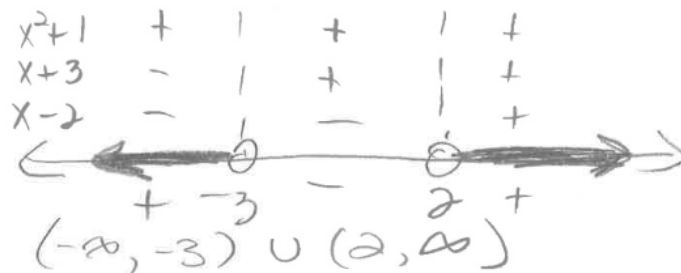
$$\frac{\cancel{(x+5)}(x-5)}{\cancel{x+5}} \leq 0$$

$$x - 5 \leq 0$$



2.  $\frac{x^2 + 1}{x^2 + x - 6} \geq 0$

$$(x+3)(x-2)$$



3.  $\frac{x-2}{x-3} \leq \frac{1}{x+3}$

$$\frac{x-2}{x-3} - \frac{1}{x+3} \leq 0$$

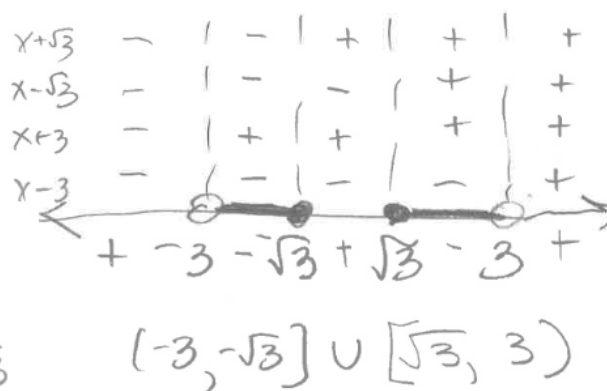
$$\frac{(x-2)(x+3) - (x-3)}{(x-3)(x+3)} \leq 0$$

$$\frac{x^2 + x - 6 - x + 3}{(x-3)(x+3)} \leq 0$$

$$\frac{x^2 - 3}{(x-3)(x+3)} \leq 0 \rightarrow x^2 = 3$$

$$x = \pm\sqrt{3}$$

$x \neq 3$      $x \neq -3$



Math 4 Honors

Unit 3 Test Review

**Station #5: Analyzing Functions without a Graphing Calculator**

Match each function rule with ALL properties that apply to that function.

Some may be used more than once.

**Functions**

**Properties**

1. C, G, K

$$f(x) = \frac{-2(x^2 + 16)}{x}$$

$x^2 + 16 = 0$   
 $\sqrt{x^2} = \sqrt{-16}$   
 $x = \pm 4i$   
 O.A.  
 $m = -2$   
 so  $-\infty \uparrow, \infty \downarrow$

- A. Has a hole when  $x = 8$ .
- B.  $x = 0$  is a zero.
- C. Has exactly two imaginary zeros.
- D. Has a vertical asymptote at  $x = 8$
- E. Has a vertical asymptote at  $x = -3$
- F. Has the  $x$ -axis as its horizontal asymptote
- G. Has an oblique asymptote
- H. Has 3 different real zeros
- I. As  $x \rightarrow \infty, f(x) \rightarrow 3$ .
- J. As  $x \rightarrow \infty, f(x) \rightarrow 1/2$ .
- K. As  $x \rightarrow \infty, f(x) \rightarrow \infty$ .
- L. Has an even multiplicity of 2.
- M. As  $x \rightarrow -3.5, f(x) \rightarrow \infty$
- N. As  $x \rightarrow 0^+, f(x) \rightarrow \infty$

2. B, E, F

$$f(x) = \frac{2x}{x^2 - 9} = \frac{2x}{(x+3)(x-3)}$$

$\rightarrow 2y = 0$   
 $x = 0$   
 H.A.  
 $y = 0$

3. A, J

$$f(x) = \frac{(x+4)(x-8)}{(2x+7)(x-8)}$$

hole when  $x = 8$

$= \frac{x+4}{2x+7} \rightarrow 2x+7 = 0$   
 $2x = -7$   
 $x = -3.5$   
 H.A.  $y = \frac{1}{2}$   
 V.A.  $x = -3.5$

4. I, N, C

$$f(x) = 3 + \frac{1}{x^2}$$

V.A:  $x = 0$   
 Local behavior

H.A:  $y = 3$

$$\frac{3x^2 + 1}{x^2}$$